Quantification of fibrous cap thickness in intracoronary optical coherence tomography with a contour segmentation method based on dynamic programming

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Abstract

Objectives. Fibrous cap thickness is the most critical component of plaque stability. Therefore, *in vivo* quantification of cap thickness could yield valuable information for estimating the risk of plaque rupture. In the context of preoperative planning and peri-operative decision making, intracoronary optical coherence tomography imaging can provide a very detailed characterization of the arterial wall structure. However, visual interpretation of the images is laborious, subject to variability, and therefore not always sufficiently reliable for immediate decision of treatment.

Methods. A novel semi-automatic segmentation method to quantify coronary fibrous cap thickness in optical coherence tomography is introduced. To cope with the most challenging issue when estimating cap thickness, namely the diffuse appearance of the anatomical abluminal interface to be detected, the proposed framework is based on a robust dynamic programming framework using a geometrical *a priori*. To determine the optimal parameters settings, a training phase was conducted on 10 patients.

Results. Validated on a dataset of 179 images from 21 patients, the present framework could successfully extract the fibrous cap contours. When assessing minimal cap thickness, segmentation results from the proposed method were in good agreement with the reference tracings performed by a medical expert (mean absolute error and standard deviation of $22 \pm 18 \ \mu\text{m}$, R=.73) and was similar to inter-observer reproducibility ($21 \pm 19 \ \mu\text{m}$, R=.74), while being significantly faster and fully reproducible.

Conclusion. The proposed framework demonstrated promising performances and could potentially be used for online identification of high risk-plaques.

Keywords Coronary artery · Optical coherence tomography · Interventional imaging · Thin-cap fibroatheroma · Contour segmentation · Dynamic programming · Preoperative planning

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1 1 Introduction

Coronary artery disease is the most common cause of human mortality and morbidity in industri-2 alized countries. Acute coronary syndrome (ACS), the most severe manifestation of atherosclerotic disease, is principally caused by acute coronary thrombosis, which is mainly provoked by plaque rupture [17]. The morphological characteristics of such plaques that are prone to rupture (also dubbed "high risk" or "vulnerable" plaques) are i) a large lipid necrotic core, ii) an overlying thin fibrous cap, and *iii*) dense macrophage infiltration (Fig. 1a) [4]. These plaques are also known as thin cap fibroatheromas (TCFAs) and are considered the precursor phenotype of plaque rupture. The most critical component of plaque stability is fibrous cap thickness, *i.e.* thinner caps being more prone to rupture than thicker caps, and the threshold of 65 μ m has been widely adopted to 10 identify high risk lesions [11]. Accordingly, identification of vulnerable plaques could potentially 11 guide appropriate surgical treatments such as percutaneous coronary intervention (e.g. balloon an-12 gioplasty or stent placement) prior to the occurrence of an event. Therefore, in vivo quantification 13 of fibrous cap thickness represents a major clinical challenge. 14

Intravascular optical coherence tomography (OCT) is a catheter-based imaging modality that 15 enables tissues to be visualized in vivo at a near-histology resolution $(10-20 \,\mu\text{m})$ and in a minimally 16 invasive way [3]. In a similar fashion as intravascular ultrasound, the inner circumference of the 17 vessel is investigated by the probe spinning along its axis while being pulled back. At each angular 18 step, a so-called A-line signal is acquired via the emission and reception of near-infrared light (center 19 wavelength of 1280 - 1350 nm). A stack of consecutive cross-sectional images along the length of 20 the assessed artery segment is then reconstructed by converting the intensity and echo time of all 21 A-lines into a gray-scale representation (Fig. 1b). The very high spatial resolution of OCT enables 22 an accurate characterization of the structure of the most superficial layers of the arterial wall, 23 and can indicate the degree of subclinical atherosclerotic lesion formation [14]. Moreover, OCT is 24 currently the only *in vivo* imaging modality with which fibrous cap thickness, the most critical 25 component of plaque stability, can be assessed accurately [10]. Therefore, OCT can potentially be 26 used for in vivo identification of high-risk plaques. 27

Although OCT images are acquired online during intervention, fibrous cap thickness quantifi-28 cation is currently performed manually offline [2, 14]. The two major drawbacks that hinder such 29 manual image analysis are i) the procedure is cumbersome and time consuming, and ii) results are 30 subject to a certain degree of variability between different analysts [9,10]. Moreover, segmentation 31 of the fibrous cap abluminal interface is a challenging task, as fibroatheromas consist of progres-32 sively unravelling tissues and are visualized in OCT as signal-poor regions with diffuse contours 33 and high signal attenuation (Fig 1a,b) [14]. Therefore, the clinical need of immediate and reliable 34 information is not fully met by current procedures based on manual image analysis. 35

Aiming to provide reliable and quantified information during OCT analysis in the interven-36 37 tion room, various (semi)automated computerized methods have recently been proposed. The attenuation coefficient of the backscattered light has been used in several classification-based ap-38 proaches [12, 16, 20]. These methods were successfully used to identify and locate different types of 39 tissues (*i.e.* healthy wall sections, lipid, calcific and fibrous tissues). Nevertheless, such techniques 40 are not devised to provide information regarding the actual delineation of anatomical interfaces, 41 and could not be used to assess fibrous cap thickness. A seminal study was proposed to specifically 42 assess fibrous cap thickness [19]. This method, based on contour segmentation by means of dynamic 43 programming was applied to extract both luminal and abluminal interfaces of the fibroatheromas, 44 and could quantify cap thickness. However, since this method did not exploit geometrical a priori 45 features, results could have potentially been hindered in images with an eccentric catheter position 46 within the lumen. Another semi-automatic method was introduced to identify the different tissue 47 types and segment the wall layers [5]. In this approach, contour segmentation was based on intensity 48 thresholding. Nevertheless, although the results of this study look promising, fibrous cap thickness 49 was not investigated per se. 50

The present study aims at introducing and evaluating a framework designed to quantify fibrous 51 cap thickness of fibroatheromas in intracoronary OCT. The principal contribution of this work is a 52 robust contour segmentation method devised to extract the fuzzy abluminal interface of the fibrous 53 cap. This novel framework is based on a dynamic programming approach that previously showed 54 successful results on the common carotid artery wall in B-mode ultrasound [24]. The accuracy 55 of the present method was validated in a set of 179 cross-sectional OCT images acquired in vivo 56 from 21 different patients, and demonstrated a similar accuracy compared to the tracings manually 57 performed by two experienced analysts. 58

⁵⁹ 2 Material and methods

The present segmentation framework is based on three principal phases, namely i) a manual ini-60 tialization aiming to indicate the presence of the fibrous cap to be analyzed, *ii*) the automatic 61 extraction of the luminal interface in the objective to localize the wall contour, and *iii*) the auto-62 matic extraction of the abluminal interface, which is subsequently exploited to assess the actual 63 cap thickness. An overview of the method is presented in Figure 1. The outline of this section is 64 the following. First, we introduce a contour segmentation scheme based on dynamic programming, 65 which is exploited in the phases (ii) and (iii) of our framework. Then, we detail the three principal 66 67 phases of our framework.

68 2.1 Dynamic programming

⁶⁹ Dynamic programming is an efficient method to find the globally optimal solution in combinatory ⁷⁰ analysis [1]. In the present context, contour segmentation is performed in the polar domain. Given ⁷¹ an image I, the anatomical interface to be extracted corresponds to a curve running from the left ⁷² to the right border of the image, as depicted in Figure 1c. We thus address the issue of determining, ⁷³ among all the potential candidate contours, the one that best describes the actual i location and ⁷⁴ ii shape (*i.e.* smoothness) of the anatomical interface. Towards this objective, we propose a specific ⁷⁵ implementation of a dynamic programming framework based on front propagation [6].

76 2.1.1 Cost function

⁷⁷ Since the anatomical interfaces to be extracted are located on regions of the image showing a strong ⁷⁸ intensity transition, the first step consists in locally enhancing the vertical intensity gradient of the ⁷⁹ image. One should notice that this transition is positive for the luminal interface (*i.e.* from dark ⁸⁰ lumen to bright tissues) and negative for the abluminal interface (*i.e.* from bright fibrous tissues to ⁸¹ dark lipid pool), as depicted in Figure 1c,d. The gradient image I_G is then built according to:

$$I_G = \pm G' * I , \tag{1}$$

with (*) the convolution operator, and G' the first derivative of a Gaussian function of standard deviation σ . The \pm sign corresponds to the gradient orientation, and is determined according to the processed interface, namely it is positive for the luminal contour, and negative for the abluminal contour. Finally, a cost function C is built such as:

$$\mathcal{C} = \mathcal{N}_{[0,1]}(-I_G) , \qquad (2)$$

with $\mathcal{N}_{[0,1]}$ representing the normalization of a set of values to the positive interval [0,1] (*viz.*: the set is first linearly scaled in such way that the minimum value becomes equal to zero, then the set is divided by the maximum value). In this image \mathcal{C} , the points most likely to represent the location of the analyzed interface correspond to the points with the lowest cost (Fig. 1e).

90 2.1.2 Front propagation

⁹¹ We now present a dynamic programming strategy to determine the path that runs in the cost ⁹² image C from left-to-right with the minimum cumulated cost \mathbb{C} . A schematic representation of this ⁹³ front propagation approach is displayed in Figure 2. The proposed approach extends a previously ⁹⁴ proposed method [23], and takes into account both the image feature (*i.e.* strong intensity gradient ⁹⁵ locally corresponding to a low cost in C) and a geometrical constraint (*i.e.* the shape *a priori* that ⁹⁶ describes a smooth structure). Therefore, high cost values as well as vertical displacement are ⁹⁷ penalized when generating the cumulated cost function \mathbb{C} , as detailed in Equation 3 (Fig. 1f).

$$\mathbb{C}(r,\theta+1) = \min_{d_r \in \{-N,\dots,0,\dots,N\}} \left\{ \mathbb{C}(r+d_r,\theta) + \left(\mathcal{C}(r,\theta+1) + \mathcal{C}(r+d_r,\theta)\right) \cdot \left(1 + \alpha \cdot d_r^\beta\right) \right\} , \quad (3)$$

⁹⁸ with (r, θ) the vertical and horizontal coordinates, d_r the vertical displacement of the path between ⁹⁹ two consecutive points, and 2N + 1 the number of reachable neighbors. The smoothness of the path ¹⁰⁰ is ruled by the positive parameters α and β . More specifically, the overall flexibility of the path is ¹⁰¹ controlled by α (*i.e.* small α values enable vertical transitions of the path, and large α values favor ¹⁰² long horizontal plateaus), and the roughness of the path is controlled by β (*i.e.* small β values yield ¹⁰³ contours that are locally spiky, and large β values impose smooth contours).

Prior to computation, the left column of \mathbb{C} (*i.e.* $\theta = 1$) is initialized to zero: in this implementation, each node on the left border acts as a seed and is a potential starting point for the final optimal path. It is also noteworthy that the weight of each candidate link depends on the cost of the edge connecting the currently evaluated node with the candidate node $(viz: C(r, \theta + 1) + C(r + d_r, \theta)$ in Eq.3), rather than the cost of the current node alone $(viz: C(r, \theta + 1))$. Therefore, this implementation is independent of the direction (*i.e.* left-to-right or right-to-left) of the front propagation.

110 2.1.3 Back tracking

In the objective to extract the globally optimal path, a back tracking scheme is adopted. Since $\mathbb C$ 111 is constructed using a penalty that depends of the vertical distance between the nodes (Eq. 3), a 112 classical gradient descent in $\mathbb C$ can not be performed to extract the minimal cost path. Instead, 113 during the previously described propagation of the front, for each node $\mathcal{C}(r, \theta + 1)$, neighboring 114 information is memorized by storing the vertical coordinate r + dr of the best candidate node C(r +115 dr, θ), as shown in Figure 2. Once the cumulated cost function \mathbb{C} is entirely built, the ending point 116 of the path is determined by the node with the minimal cumulated cost located on the right border 117 of the image. Finally, the total path is extracted via back tracking by iteratively connecting the 118 nodes using the stored neighboring information, from the right to the left border of the image. 119

¹²⁰ 2.2 Initialization and pre-processing

The present framework starts with the user manually performing a quick and simple initialization phase. For a given pullback, this operation consists in i) visually detecting the presence of a necrotic core covered by a fibrous cap, and ii) manually indicating the region of interest (ROI) to be analyzed. The ROI was defined by an arc encompassing the fibrous cap, as displayed in Figure 1a,b. After this operation has been performed, the region shadowed by the guidewire is easily masked out using an approach similar to the one proposed in [19].

127 2.3 Lumen segmentation

The luminal interface is represented by a positive intensity transition (*i.e.* from dark lumen to bright (i.e. from dark lumen to bright

tissues) and is generally well perceptible. The luminal contour is easily extracted by applying the previously described dynamic programming approach to the image I.

131 2.4 Abluminal interface segmentation

The abluminal interface is represented by a negative intensity transition (*i.e.* from bright fibrous 132 tissues to dark lipid pool) and is generally more diffuse and fuzzy. Prior to applying the dynamic 133 programming segmentation method, the ROI manually selected by the user is extracted from the 134 image I, as depicted in Figure 1c. Then, a spatial transformation T is applied to the ROI. The aim 135 of this transformation T is to generate a sub-image \mathcal{C}_T in which the luminal interface corresponds 136 to a straight horizontal line in the polar domain (Fig. 1e). The cost function \mathcal{C} is thus shifted line-137 by-line to match the vertical origin with respect to the luminal contour rather than to the probe 138 location. The rationale of our approach is based on the fact that, as the fibrous cap thickness does 139 not undergo large variations within adjacent sites, we can exploit a geometrical a priori to cope with 140 the diffuse appearance of the anatomical interface. In the transformed sub-image C_T , the abluminal 141 contour that needs to be extracted is henceforth expected to correspond to a nearly-horizontal 142 structure. Subsequently, the dynamic programming segmentation method is applied to C_T . Finally, 143 the actual location of the abluminal interface in the original image is determined by applying the 144 corresponding inverse spatial transformation T^{-1} onto the extracted optimal path (Fig. 1g). 145

146 3 Experiments

¹⁴⁷ 3.1 Data collection and study population

The OCT imaging database of Thoraxenter, Erasmus MC (Rotterdam, The Netherlands) was 148 screened for native coronary artery OCT pullbacks containing fibroatheromas. Fibroatheromas 149 were defined as necrotic core containing regions with the maximum circumferential extent (arc) ex-150 ceeding one quadrant of the cross-section. Thirty one patients (mean age 61.3 ± 8.4 y.o., 25 males) 151 suffering from coronary artery disease were randomly selected from the database and included in 152 our study. The only inclusion criteria was the presence of fibroatheromas in the acquired pullbacks. 153 Informed consent was acquired from the patients for use of their imaging data. All procedures 154 followed were in accordance with the ethical standards of the responsible committee on human 155 experimentation (institutional and national) and with the Helsinki Declaration of 1975, as revised 156 in 2008 (5). Pullbacks were acquired in the catheterization laboratory of Erasmus MC for clinical 157 indications, using the C7XR frequency-domain system and the Dragonfly intracoronary imaging 158 catheter (Lightlab/St Jude, Minneapolis, MN, USA). Image acquisition was performed with a pre-159 viously described non-occlusive technique [14]. Briefly, after positioning the OCT catheter distally 160 to the segment of interest, it was pulled back automatically at 20 mm/s with simultaneous con-161 trast infusion through the guiding catheter by a power injector (flush rate 3 - 4 ml/s). Images 162 were acquired at the rate of 100 frames/s (corresponding to 54000 A-lines/s), over an average total 163 length of 54 mm along the vessel, resulting in a stack of 271 frames. The central bandwidth of the 164 near-infrared light was 1310 nm, and the spatial resolution of the system was 20 μ m and 30 μ m in 165 the axial and lateral directions, respectively. The depth of the scan range was 4.3 mm, and acquired 166 images were sampled at 504 \times 968 pixels per frame, with an isotropic pixel size of 4.5 μm . 167

¹⁶⁸ 3.2 Image analysis procedure

¹⁶⁹ For each analyzed pullback, an analyst A_1 selected a series of consecutive images where a necrotic

¹⁷⁰ core with an overlying fibrous cap could be observed visually. Definition of image features identify-¹⁷¹ ing a necrotic core was signal-poor regions with diffuse contours and high signal attenuation [14].

¹¹² Ing a horototic core was signal poor regions with analyce contours and high signal accontation [11]. ¹²² Subsequently, A_1 indicated, in each selected frame, the limits of the ROI encompassing the fibrous

173 cap (Fig. 1a,b). All that information was stored, and subsequently used by the automatic seg-

¹⁷⁴ mentation method, the expert A_1 , as well as an additional analyst A_2 to perform, blinded to the

results of others, the extraction of the abluminal interface of the fibrous cap. All tracings realized by the human analysts were performed in the Cartesian domain *via* an effective graphical interface that was developed in-house for this purpose. The two experts are specialists in vascular imaging and OCT. They received identical instructions and were trained on the new segmentation software during 1 month prior to this study.

180 3.3 Parameters settings

181 3.3.1 Luminal interface

¹⁸² Segmentation of the luminal interface does not present any particular challenge. The proposed ¹⁸³ segmentation framework was therefore applied on the entire circumference of all images with the ¹⁸⁴ following heuristically-determined parameters settings: smoothness parameters, $\alpha = 0.1$ and $\beta = 1$; ¹⁸⁵ standard deviation of the Gaussian filter, $\sigma = 90 \ \mu$ m; number of reachable neighbors, 2N + 1 = 41.

186 3.3.2 Abluminal interface

Aiming to accurately extract the abluminal contour of the fibrous cap, the optimal parameters 187 settings were determined by means of a training phase. In this purpose, a training set was generated 188 by randomly selecting a sub-sample of $\Omega_1 = 10$ pullbacks among the cohort of 31 participants. 189 During the training phase, the proposed framework was repeatedly applied to the training set, 190 with 1000 different sets of $\{\alpha, \beta, \sigma\}$ parameters settings, as displayed in Table 1. The number 191 2N + 1 of reachable neighbors was equal to 41 to reduce the search space while still allowing the 192 path to follow the curvature of the analyzed interface. A score was then attributed to each set of 193 parameters settings, by calculating, for every frame of the training set, the mean error between the 194 reference abluminal contour manually traced by \mathcal{A}_1 and the corresponding segmentation contour 195 resulting from the proposed framework. Finally, the optimal set of $\{\alpha, \beta, \sigma\}$ parameters settings 196 was determined by visually inspecting the contours of the 10 best ranked sets, and selecting the 197 configuration yielding the contours with the most realistic appearance. The selected configuration 198 was the 9th best ranked set, with a mean absolute error of $32\pm40 \,\mu\text{m}$. The parameters corresponding 199 to the chosen set were as follow: smoothness parameters, $\alpha = 0.2$ and $\beta = 1.8$; standard deviation 200 of the Gaussian filter, $\sigma = 45 \ \mu m$. For comparison purpose, the mean absolute error corresponded 201 to $31 \pm 41 \ \mu\text{m}$ for the best ranked set $(\{\alpha, \beta, \sigma\} = \{0.4, 1.0, 36 \ \mu\text{m}\})$, and to $57 \pm 74 \ \mu\text{m}$ for the worst 202 ranked set ($\{\alpha, \beta, \sigma\} = \{2.0, 2.0, 9 \ \mu\text{m}\}$). Moreover, the difference between the errors distributions 203 corresponding to the chosen set and the best ranked set yielded a zero bias and a 95% confidence 204 interval equal to $[-3,3] \mu m$. By defining a zone of clinical indifference equal to $9 \mu m$ (*i.e.* ± 1 pixel), 205 we can conclude that the accuracy of the chosen set is statistically equivalent to the accuracy of 206 the best ranked set. Resulting errors in function of the $\{\alpha, \beta, \sigma\}$ parameters settings are displayed 207 208 in Figure 3.

209 3.4 Fibrous cap thickness evaluation

The performance of the proposed segmentation framework was evaluated as follow: a testing set was generated with the remaining $\Omega_2 = 21$ pullbacks, then the segmentation framework was applied onto the testing set with the previously determined optimal parameters settings. For each analyzed image, thickness of the fibrous cap was assessed in the Cartesian domain, for our automatic method as well as the two analysts \mathcal{A}_1 and \mathcal{A}_2 . For a given point of the abluminal interface of the fibrous cap, the measure was performed on the line going through the center of the lumen and the assessed point. Cap thickness corresponded to the distance between the two points defined by the intersection of ²¹⁷ this line with both luminal and abluminal interfaces. For each image, two different measurements

- ²¹⁸ were realized to evaluate cap thickness, namely *i*) as a vector describing each A-line of the analyzed
- ²¹⁹ ROI, and *ii*) as the thinnest portion within the frame.
- 220 3.5 Manual correction of the abluminal contour

The robustness of the proposed segmentation method was also evaluated in the training set by 221 the expert A_2 visually assessing each resulting segmentation contour of the abluminal interface, 222 and manually correcting it if necessary. More precisely, one or several control points were manually 223 placed by \mathcal{A}_2 to correct the automatic segmentation when the analyst did not agree with the orig-224 inal resulting contour. The corrected segmentation contour was generated by means of a modified 225 implementation of the dynamic programming method detailed in Section 2.1. Immediately after 226 the generation of the cost function \mathcal{C} , a modified cost function \mathcal{C}' was built using the following 227 approach. For each manually defined control point $p(\theta, r)$, the node (θ, r) of the cost function \mathcal{C}' 228 was set to zero, and all other nodes of the column θ were set to an infinity value (Fig. 2). The 229 following steps of the dynamic programming method were then applied to the cost function \mathcal{C}' . As 230 a consequence, the resulting contour corresponded to a path going through all the control points 231 while still performing a search in the regions that were not corrected¹. 232

233 4 Results

Among the 31 involved patients, the average number of analyzed images per individual pullback 234 was 8.4 ± 1.7 (range 5 - 10) consecutive frames, with a total of 261 analyzed images. The average 235 length of the analyzed arc per image was $30\pm16\%$ of the entire vessel circumference (range 4-78%). 236 The training set was generated with $\Omega_1 = 10$ random pullbacks (corresponding to 82 images), and 237 the testing set was generated from the remaining $\Omega_2 = 21$ pullbacks (corresponding to 179 images). 238 For each analyzed frame of both training and testing sets, the luminal interface was automat-239 ically extracted for the entire vessel circumference, and the abluminal interface of the fibrous cap 240 was automatically extracted within the ROI defined by the expert \mathcal{A}_1 (Fig. 1a,b). Representative 241 examples of resulting segmentation contours are displayed in Figure 4. The results of our segmen-242 tation method, compared to the tracings of both observers \mathcal{A}_1 and \mathcal{A}_2 , are presented alongside to 243 the corresponding inter-observer variability in Table 2. 244

Quantification of fibrous cap thickness was derived from the segmented contours of both luminal 245 and abluminal interfaces. Including each analyzed A-line per frame, the average cap thickness was 246 $210 \pm 82 \ \mu m$ for the 179 images of the testing set, and $228 \pm 88 \ \mu m$ for the 82 images of the training 247 set. The mean minimal cap thickness (*i.e.* the thinnest point in a given frame) was $126 \pm 37 \ \mu m$ 248 for the testing set, and $161 \pm 64 \ \mu m$ for the training set. Results of cap thickness derived from the 249 automatic framework were evaluated against the manual references performed by the two analysts, 250 as presented in Table 3. The Bland-Altman plots (Fig. 5) show an overall good agreement between 251 the present method and the two experts when assessing minimal cap thickness. 252

It is also insightful to quantify the absolute error of the proposed segmentation framework normalized by the cap thickness. Calculating, for each analyzed A-line, the ratio between the absolute segmentation error and the corresponding cap thickness, and putting all these ratios together, the mean values were $16 \pm 19\%$ for the 179 images of the testing set, and $15 \pm 22\%$ for the 82 images of the training set. When calculating the relative errors corresponding to the minimal cap thickness, the mean values were $19 \pm 18\%$ for the testing set, and $24 \pm 31\%$ for the training set.

¹ Please note that in the remaining of this manuscript, any reference to segmentation contour as well as all results are related to the original automatic contours (*i.e.* non manually corrected), except when explicitly specified.

Reviewing the resulting abluminal interface segmentation contours of the testing set, the ex-259 pert \mathcal{A}_2 performed a correction of the automatic contours with which he disagreed, as detailed in 260 Section 3.5. A total of 20 frames out of 179 was corrected, corresponding to 7 pullbacks out of 21. 261 For all these corrected frames, the mean number of manually added control points was 1.8 ± 1.1 262 (range 1-4). The two main factors motivating this manual corrections were *i*) image artifacts 263 hampering the automatic segmentation, and ii) the presence of several interface-like structures 264 attracting the contour. Examples of such manual correction of erroneous contours are depicted 265 in Figure 6. Assessing the fibrous cap with the corrected contours yielded an overall reduced cap 266 thickness (bias of $-26 \ \mu m$, Bland-Altman 95% limits of agreement of $[-95, 147] \ \mu m$). Comparing, 267 for the 20 corrected frames, the bias (and 95% limits of agreement) of the cap thickness estimation 268 resulting from the automatic segmentation and the manually corrected segmentation, it decreased 269 from 22 μ m ([-142, 187] μ m) to -4 μ m ([-125, 117] μ m) when evaluated against the reference trac-270 ings of \mathcal{A}_2 , but increased from 1 μ m ([-133, 134] μ m) to -26 μ m ([-159, 108] μ m) with \mathcal{A}_1 . This 271 discrepancy, reflecting the subjectivity of human analysts, is also visible through the bias between 272 the two experts, which was equal to 21 μ m ([-124, 166] μ m) in these 20 frames. 273

As for the computational speed, the present framework required on average 2 s to perform the contour extraction of both luminal and abluminal interfaces and evaluate its thickness for a single image, while the corresponding manual operation required on average 190 s. In both cases and additionally, the average time (per frame) required by the user to define the ROI was 20 s.

278 5 Discussion

The principal aim of this study was to introduce a contour segmentation method devised to quantify fibrous cap thickness in cross-sectional OCT images. Since cap thickness is the most critical component of plaque stability [11], its quantification is likely to provide crucial information about the risk of plaque rupture. The proposed framework was trained in 82 images from 10 patients, and subsequently validated in 179 images from 21 other patients.

The evaluation of the proposed segmentation framework was conducted against reference seg-284 mentation contours manually generated by two expert analysts in a set of 179 images. The mean 285 absolute error of the automatic method versus both analysts (i.e. $22 \pm 18 \ \mu m$ and $26 \pm 22 \ \mu m$) was 286 similar to the inter-observer variability (*i.e.* $21 \pm 19 \ \mu m$), as presented in Table 3, which indicates 287 that the present method performs at least as well as an experienced observer when assessing the 288 cap thickness. It is also noteworthy that these errors are relatively small compared to the spatial 289 resolution of the system, which was 20 μ m. When assessing the thinnest portion of the fibrous cap 290 in the image, an overall low positive bias was observed between the automatic method and the 291 experts (*i.e.* 8.4 μ m w.r.t. A_1 , and 4.6 μ m w.r.t. A_2), showing that cap thickness is slightly over-292 293 estimated by the computerized method. Furthermore, an accuracy improvement of roughly 30% could be observed when quantifying, in a given frame, the thinnest portion of the cap rather than 294 the overall thickness of the entire cap (*i.e.* $22 \pm 18 \ \mu m \ v.s. \ 30 \pm 37 \ \mu m$, Table 3). This performance 295 discrepancy can be explained by the fact that thinnest portions tend to present sharper and more 296 defined contours, whereas thickest portions of the cap often present more fuzzy contours (*i.e.* due to 297 a greater attenuation of the signal in deeper tissues, or to a decrease of the lateral spatial definition 298 along the distance from the probe in the Cartesian domain). We consider the higher accuracy in 299 detection of minimal cap thickness favorable, as the minimal value of cap thickness is the most 300 clinically relevant information [11]. It is also noteworthy that the ability of OCT to quantify cap 301 thickness was previously evaluated in a study where cap thickness was measured manually in OCT 302 images and compared to the corresponding ex vivo histopathologic segments [10]. Results from that 303 study demonstrated a mean signed error of $-22 \pm 44 \ \mu m$ when measuring the thinnest portion of 304 the cap. This magnitude can thus be understood as the systematic uncertainty that is introduced 305 when analyzing cap thickness in OCT images. The level of accuracy of the proposed method can 306

³⁰⁷ be validated by the fact that the mean signed error is small in comparison to that uncertainty, ³⁰⁸ namely $-8.4 \pm 28 \ \mu m$ (Table 3).

A training phase was carried out on a sub-sample of $\Omega_1 = 10$ pullbacks to determine the 309 optimal set of the $\{\alpha, \beta, \sigma\}$ parameters for the extraction of the fibrous cap abluminal interface. 310 311 Despite the fact that the method was optimized with respect to the manual tracings of the expert 312 \mathcal{A}_1 , results show that the errors of the automatic method *versus* both analysts were close to each 313 other as well as to the inter-observer variability, for contour segmentation (Table 2) as well as cap 314 thickness assessment (Table 3). Moreover, both automatic and manual errors generated from the training set were similar to the errors resulting from the testing phase (Tables 2 and 3), which 315 confirms the robustness of the proposed framework against new images. In a few challenging cases 316 (i.e. 20 images out of 179), automatic segmentation of the abluminal interface failed, due to the 317 presence of bright image artifacts or several interface-like structures. To cope with these issues, 318 a correction scheme was proposed. This task is performed easily and quickly by the user visually 319 assessing the resulting segmentation, and indicating, if necessary, one or several control points to 320 modify the contour, as displayed in Figure 6. As opposed to the abluminal contour, segmentation 321 of the luminal interface does not present any particular challenge, as the location of the anatomical 322 boundary is well perceptible (Fig.1b). This is testified by the fact that the parameters settings 323 used for the luminal segmentation assign less weight on the shape constraint and more weight on 324 the image data (*i.e.* $\{\alpha, \beta, \sigma\} = \{0.1, 1.0, 90 \ \mu\text{m}\}$), compared to the abluminal parameters settings 325 $(i.e. \{\alpha, \beta, \sigma\} = \{0.2, 1.8, 45 \ \mu m\}).$ 326

The clinical context of our work relates to peri-operative decision making rather than patient 327 screening: the severity of the case is averred and invasive imaging is required. The rationale of the 328 present study is to assess plaque stability via quantifying the thickness of the overlying fibrous 329 cap. Indeed, it has been demonstrated that cap thickness is the most critical component of plaque 330 stability [11], and that lesion morphology is associated with future events [13]. The error introduced 331 by the present framework when assessing minimal cap thickness corresponded to $22 \pm 18 \ \mu$ m. This 332 is relatively large compared to the threshold of 65 μ m used to identify rupture-prone sites [17]. 333 Nevertheless, the error of the automatic method was similar to the agreement between the two 334 experts, which was $21 \pm 19 \ \mu m$. One should also notice that the empirical 65 μm threshold may 335 be under-evaluated, since ex vivo tissues can undergo variable shrinkage rate during histological 336 preparation [14, 17]. Indeed, it has recently been demonstrated that ruptured plaques in ACS are 337 often associated with a fibrous cap thickness of up to 100 μ m [15], and that the best cut-off to 338 predict rupture was 151 μ m for most representative fibrous caps [21]. Accordingly, the clinical 339 applicability of the proposed method is supported by a relatively accurate quantification of cap 340 thickness. 341

To the best of our knowledge, the study presented by Wang et al. [19] is the only one to report a 342 semi-automatic segmentation scheme dedicated to quantify fibrous cap thickness in coronary OCT. 343 The accuracy of that method was slightly better than that of the present framework, namely the 344 mean absolute errors (\pm standard deviation) were 25 (\pm 31) μ m vs 31 (\pm 38) μ m for the abluminal 345 interface of the cap, and 27 (± 27) $\mu m vs$ 30 (± 37) μm for the overall cap thickness. Nevertheless, 346 the pertinence of such comparison is limited by the fact that our method was applied onto a 347 different dataset, using a different OCT scanner, and that the protocol followed by the expert A_1 348 to determine the fibrous caps to be analyzed may also have differed. Moreover, the finding of a 349 higher inter-observer variability as well in our study could imply the presence of challenging cases 350 in our dataset. 351

A limitation of this study is that the cap thickness validation was performed against tracings manually generated by expert analysts, but not against *ex vivo* histopatholgic specimens. Therefore, the actual ground truth is lacking, and further validation is warranted. However, as a variable shrinkage rate often occur during histological preparation of the tissues [14, 17], validation on *ex vivo* data is also expected to involve a certain amount of uncertainty. Another limitation of this study is that a manual initialization phase is required to be performed by the user to indicate the

location of the ROI encompassing the fibrous cap to be analyzed. A certain amount of variability 358 is to be expected in between two selections from the same experts, or in between the selection 359 of two different experts, thus hindering clinical applicability. This could be remedied by a more 360 automated way of detecting these locations. Therefore future work will focus on fully-automatic 361 detection of such diseased regions, using an approach based on machine learning [22]. One should 362 also notice that, since the spatial resolution along the z-axis is rather coarse compared to the axial 363 resolution (*i.e.* 200 μ m vs 20 μ m), a three-dimensional segmentation approach is not expected to 364 greatly improve the overall accuracy. For this reason, the proposed framework is based on two-365 dimensional cross-sectional images. This issue could be addressed in further work by upsampling 366 the acquired data using an ultrafast OCT system at 3200 frames per second [18]. To cope with the 367 diffuse appearance of the abluminal contours, multiple texture features could also be extracted in 368 addition to the intensity gradient in order to generate a multi-dimensional cost function \mathcal{C} . Future 369 perspectives will also aim at investigating the association of wall shear stress with cap thickness 370 using a fusion of imaging parameters with OCT and biplane angiography, in the objective to assess 371 the risk of plaque rupture with improved performances. Potential applications could also include 372 automated assessment of device-induced vascular responses [7, 8]. 373

374 6 Conclusion

The context of this study is to assess rupture-prone plaques by quantifying the thickness of the 375 overlying fibrous cap in cross-sectional coronary OCT imaging. A segmentation framework devised 376 to extract the contours of the cap was proposed. In the objective to localize the diffuse and fuzzy 377 abluminal interface, the introduced method is based on a specific dynamic programming approach 378 that integrates a geometrical a priori. Validated on in vivo data in 21 patients suffering from 379 coronary artery disease, the method provided robust and accurate results, in a clinically acceptable 380 computational time. The automatic framework performed as well as two expert analysts, while being 381 substantially faster. Accordingly, the proposed approach could provide a useful aid for interventional 382 planning and decision making in the catheterization laboratory. 383

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- **Conflict of interest** The authors declare that they have no conflict of interest.

386 Figures



Fig. 1 Segmentation framework. (a) Cartoon depicting the region of interest (ROI, dashed lines) encompassing the fibrous cap. (b) OCT image of an *in vivo* human coronary artery, in Cartesian coordinates, with the resulting luminal (cyan line) and abluminal (magenta line) segmentation contours. (c) ROI in polar coordinates, with the luminal contour (cyan line). (d) Gradient image I_G . (e) Transformed cost image C_T . (f) Cumulated cost \mathbb{C} , with the optimal path (magenta line). (g) Resulting abluminal segmentation contour.



Fig. 2 Schematic representation of the front propagation scheme, corresponding to the panel (f) in Figure 1. (a) Original polar image, with the pixels represented by the nodes (in this example, the layout is coarse for improved visibility). (b) Left-to-right front propagation, with the current location of the front indicated by the vertical dashed line. The current node is indicated by an asterisk, and the connected gray nodes correspond to the set of potential neighbors. In this example, the number 2N + 1 of horizontally reachable neighbors is equal to 3. The black lines connecting the nodes represent the successive back-tracking steps from a given node to the left border of the image. Please note that in the case of segmenting the luminal interface, the nodes of the upper row correspond to the top of the polar image (as shown in this example), whereas in the case of the segmenting the abluminal interface, the nodes of the upper row correspond to the luminal interface.



Fig. 3 Mean absolute segmentation error of the fibrous cap abluminal interface, between the automatic framework and the manual tracings of the analyst A_1 , in function of the parameters settings $\{\alpha, \beta, \sigma\}$. In each panel, the location of the minimal error is indicated by the black dot.



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Fig. 4 Representative results of the segmentation framework on 8 frames from different pullbacks. For each example, the panel composition is the following. The top row displays the full image with the region of interest (ROI, white arc). The middle row displays an enlarged view of the region delimited by the dashed square in the top row. The automatic lumen segmentation is represented by the cyan line. Within the ROI, tracings of the abluminal interface performed by the segmentation method and the analysts A_1 and A_2 are represented by the magenta, yellow and green lines, respectively. The bottom row displays the cap thickness (scale in μ m), automatically computed within the ROI as the distance between the luminal and abluminal contours that were extracted by the segmentation method.

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Fig. 5 Bland-Altman plots, comparing the results of minimal cap thickness assessed in the training set, for the proposed automatic method and the manual tracings performed by the two analysts A_1 and A_2 . The solid and dashed lines represent the bias and the 95% limits of agreement, respectively.



Fig. 6 Example of manual contour correction, on 4 frames from different pullbacks. The top, middle and bottom rows display the original image, the automatic segmentation contour of the fibrous cap (orange line), and the corrected segmentation contour (magenta line), respectively. In the bottom row, the control points that were manually indicated by the analyst are represented by the black dots.

387 Tables

 Table 1
 Values of the parameters settings used during the training phase of the method.

Parameter	Number of	Min	Max	Increment step
	different values			
α	10	0.2	2.0	0.2
β	10	0.2	2.0	0.2
σ	10	$9~\mu{ m m}$	$90~\mu{ m m}$	$9~\mu{ m m}$

Table 2 Absolute segmentation errors (mean \pm standard deviation) of the abluminal interface of the fibrous cap, for the automatic method (Auto) and the two analysts (A_1 and A_2).

Errors (μm)	Auto vs \mathcal{A}_1	Auto vs \mathcal{A}_2	$\mathcal{A}_1 vs \mathcal{A}_2$
Testing set $(\Omega_2 = 21)$	31 ± 38	37 ± 41	30 ± 39
Training set $(\Omega_1 = 10)$	31 ± 39	33 ± 33	34 ± 43

Table 3 Evaluation of fibrous cap thickness, with absolute error (mean \pm standard deviation), bias, 95% limits of agreement (Lim), and Pearson coefficient (R), for the automatic method (Auto) and the two analysts (A_1 and A_2).

Errors (µm)	Overall cap thickness over the entire ROI			Minimal cap thickness per frame				
	Absolute	Bias	Lim	R	Absolute	Bias	Lim	R
Testing set $(\Omega_2 = 21)$								
Auto $vs \mathcal{A}_1$	30 ± 37	1.4	[-92, 95]	.85	22 ± 18	8.4	[-46, 63]	.73
Auto $vs \mathcal{A}_2$	36 ± 41	4.9	[-101, 111]	.81	26 ± 22	4.6	[-61, 70]	.62
$\mathcal{A}_1 vs \mathcal{A}_2$	36 ± 41	3.6	[-102, 109]	.82	21 ± 19	-3.8	[-59, 52]	.74
Training set $(\Omega_1 = 10)$								
Auto $vs \mathcal{A}_1$	31 ± 39	-1.4	[-99, 96]	.86	30 ± 27	2.4	[-77, 82]	.82
Auto $vs \mathcal{A}_2$	32 ± 33	-1.8	[-91, 87]	.87	29 ± 27	2.0	[-75, 79]	.85
$\mathcal{A}_1 vs \mathcal{A}_2$	35 ± 41	-0.4	[-105, 105]	.84	24 ± 25	-0.4	[-68, 67]	.89

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