

# Inside ARToolKit

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# But

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- **40 min. is too short to talk everything.**
- **Focus into some important points.**
- **This is for people who has developed applications with ARToolKit.**

# Outline

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## 1. Mathematical & Algorithm Background

- **Pose & Position Estimation**
- **Rectangle Extraction**

## 2. Implementation

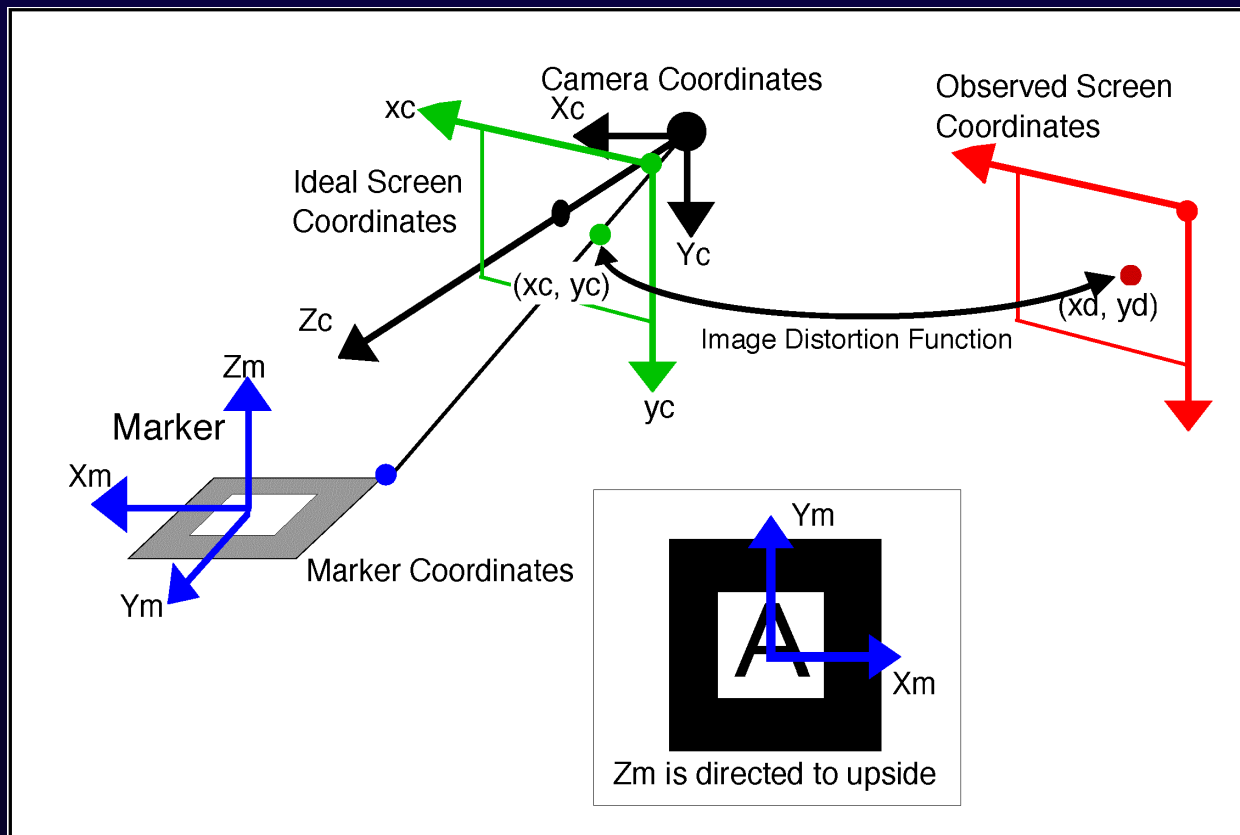
- **Camera Calibration**
- **Image Processing**
- **Pose Estimation**
- **Background Video Stream Display**

# 1.1 Pose & Position Estimation

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- **Coordinates System**
- **Equations**
- **Calculation**
- **Initial Condition Problem**

# Coordinate Systems



# Relationships: Marker & Camera

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## Rotation & Translation

$$\begin{bmatrix} X_C \\ Y_C \\ Z_C \\ 1 \end{bmatrix} = \begin{bmatrix} R_{11} & R_{12} & R_{13} & T_1 \\ R_{21} & R_{22} & R_{23} & T_2 \\ R_{31} & R_{32} & R_{33} & T_3 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_M \\ Y_M \\ Z_M \\ 1 \end{bmatrix}$$

$$= \mathbf{T}_{CM} \begin{bmatrix} X_M \\ Y_M \\ Z_M \\ 1 \end{bmatrix}$$

# Relationships: Camera & Ideal Screen

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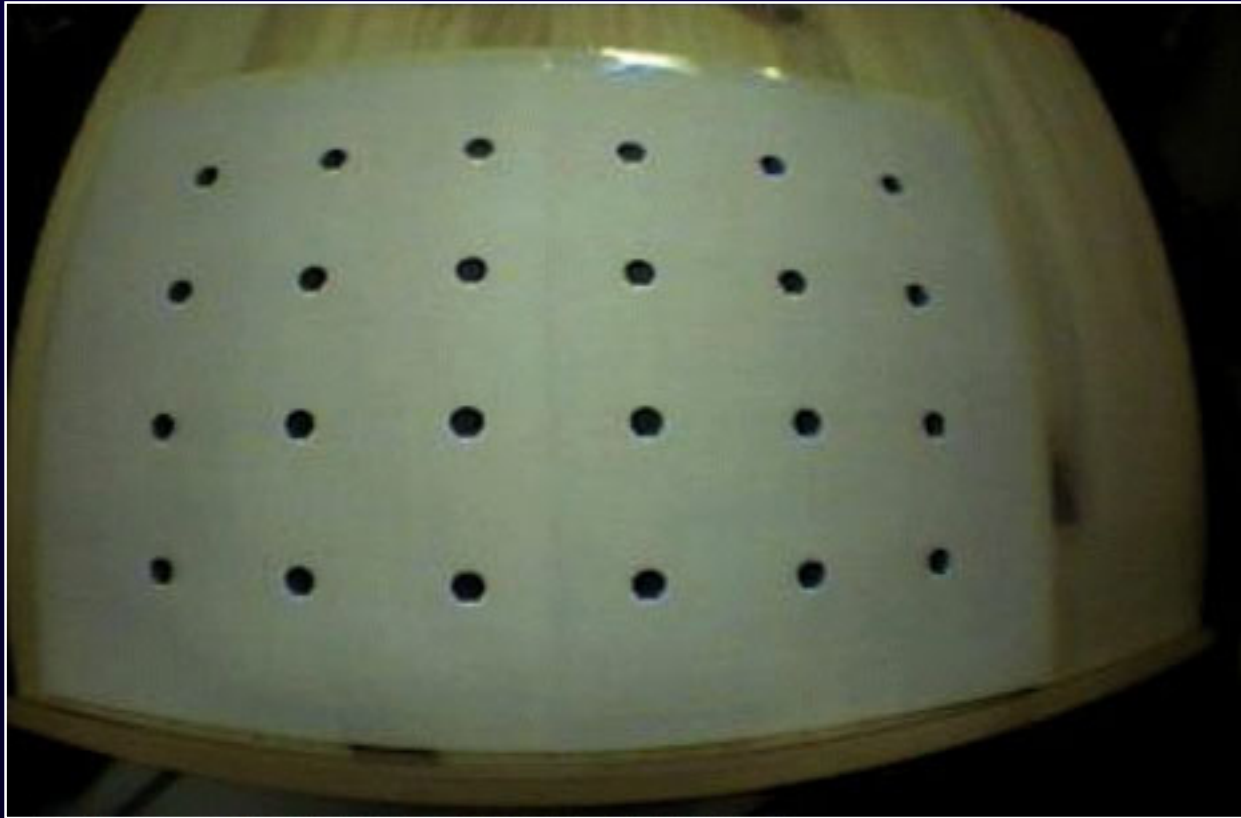
## Perspective Projection

$$\begin{bmatrix} hX_I \\ hY_I \\ h \end{bmatrix} = \begin{bmatrix} sf_x & 0 & x_c & 0 \\ 0 & sf_y & y_c & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} X_C \\ Y_C \\ Z_C \\ 1 \end{bmatrix} = \mathbf{C} \begin{bmatrix} X_C \\ Y_C \\ Z_C \\ 1 \end{bmatrix}$$

$\mathbf{C}$  : Camera Parameter

# Image Distortion

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# Image Distortion Parameters

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## Relationships between Ideal and Observed Screen Coordinates

$$d^2 = (x_I - x_0)^2 + (y_I - y_0)^2$$

$$p = \{1 - fd^2\}$$

$$x_O = p(x_I - x_0) + x_0, \quad y_O = p(y_I - y_0) + y_0$$

$(x_0, y_0)$  : Center Coordinates of Distortion

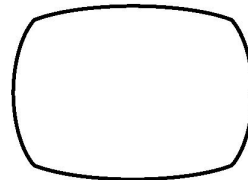
$f$ : Distortion Factor

# Scaling Parameter for Size Adjustment

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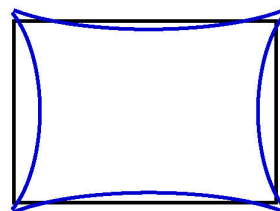
Ideal Image



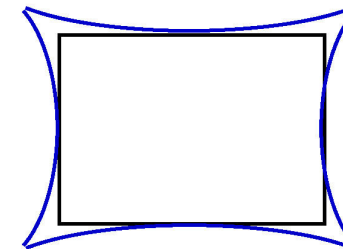
Distorted Image



Observed Image



Compensated Image  
(doesn't fit the screen)



Scale adjusted Image

# Implementation of Image Distortion parameters

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$$x = s(x_i - x_0), y = s(y_i - y_0)$$

$$d^2 = x^2 + y^2$$

$$p = \{1 - fd^2\}$$

$$x_d = px + x_0, \quad y_d = py + y_0$$

$$\text{dist\_factor}[0] = x_0$$

$$\text{dist\_factor}[1] = y_0$$

$$\text{dist\_factor}[2] = 1000000000.0 * f$$

$$\text{dist\_factor}[3] = s$$

# What is pose & position estimation?

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Marker Coordinates:  $(X_m, Y_m, Z_m)$



$T_{mc} : ?????$

**KNOWN**

Camera Coordinates



**KNOWN**

Ideal Screen Coordinates

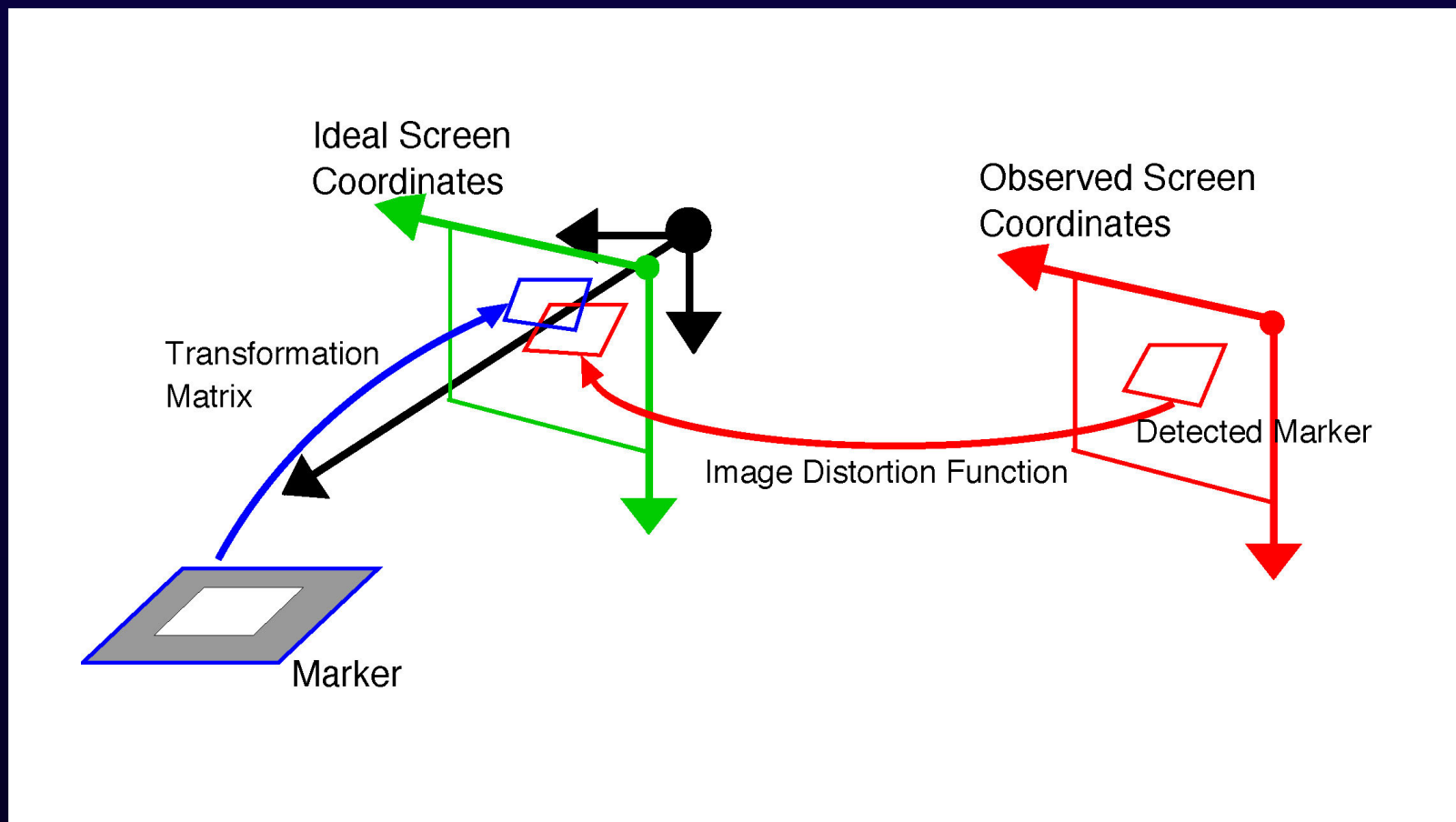


**KNOWN**

**GET by Image Processing**

Observed Screen Coordinates:  $(x_o, y_o)$

# How to get $T_{CM}$



# Search $T_{cm}$ by Minimizing Error

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## Optimization

- Iterative process

$$\begin{bmatrix} h\hat{x}_i \\ h\hat{y}_i \\ h \end{bmatrix} = \mathbf{C} \cdot \mathbf{T}_{CM} \begin{bmatrix} X_{Mi} \\ Y_{Mi} \\ Z_{Mi} \\ 1 \end{bmatrix}, \quad i = 1, 2, 3, 4$$

$$err = \frac{1}{4} \sum_{i=1,2,3,4} \left\{ (x_i - \hat{x}_i)^2 + (y_i - \hat{y}_i)^2 \right\}$$

# How to set the initial condition for optimization process

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## Geometrical calculation based on 4 vertices coordinates

- Independent in each image frame: Good feature.
- Unstable result (Jitter occurs.): Bad feature.

## Use of information from previous image frame

- Needs previous frame information.
- Cannot use for the first frame.
- Stable results. (This does not mean accurate results.)

**ARToolKit supports both.**

**See 'simpleTest2'.**

## 1.2 Rectangle Extraction

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1. Thresholding, Labeling, Feature Extraction (area, position)
2. Contour Extraction
3. Four straight lines fitting



- Little fitting error => Rectangle.

This method is very simple. Then it works very fast.



## 2. Implementation

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- Camera Calibration Method
- Image Processing
- Pose Estimation
- Background Video Stream Display

## 2.1 Camera Calibration

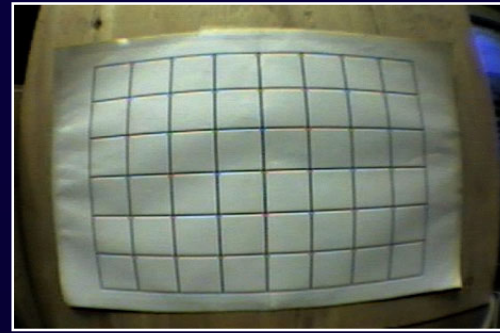
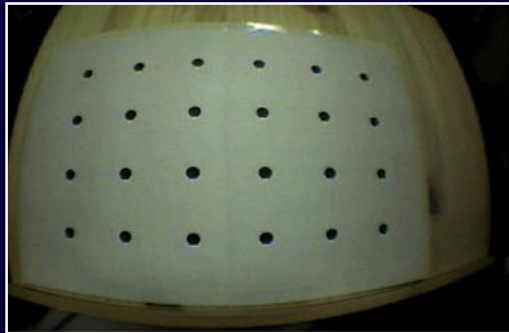
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- **Camera Parameters**
  1. Perspective Projection Matrix
  2. Image Distortion Parameters
- **ARToolKit has 2 methods for camera calibration.**
  1. Accurate 2 steps method
  2. Easy 1 step method

# Accurate 2 steps method

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Using dot pattern and grid pattern

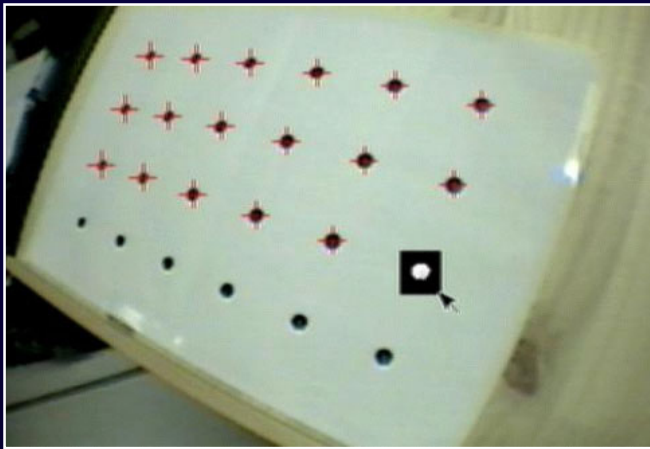


## 2 step method

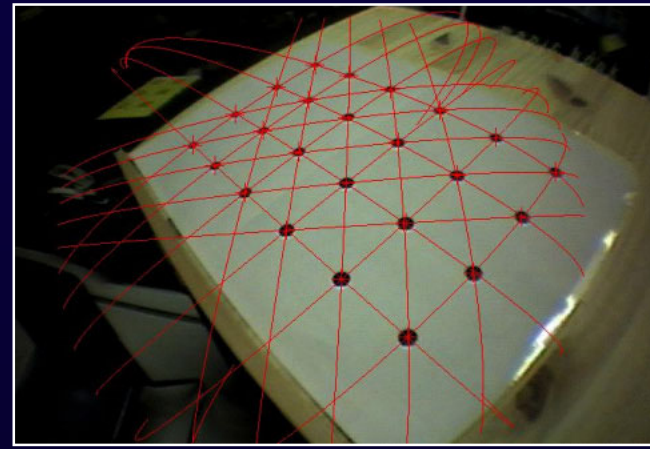
- 1) Getting distortion parameters
- 2) Getting perspective projection parameters

# Step 1: Getting distortion parameters 'calib\_dist'

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**Selecting dots with  
mouse**

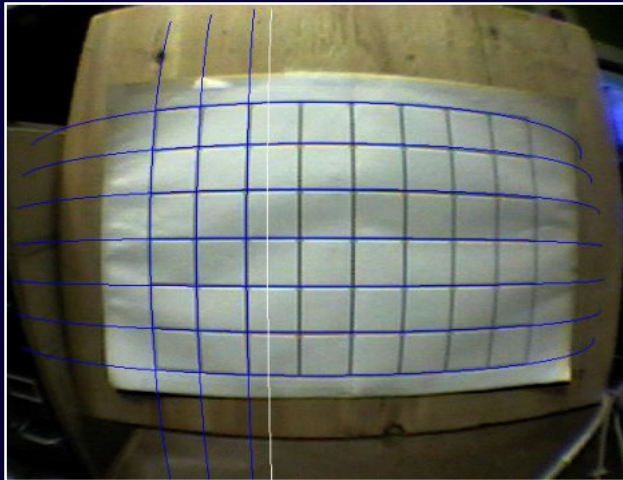


**Getting distortion parameters  
by automatic line-fitting**

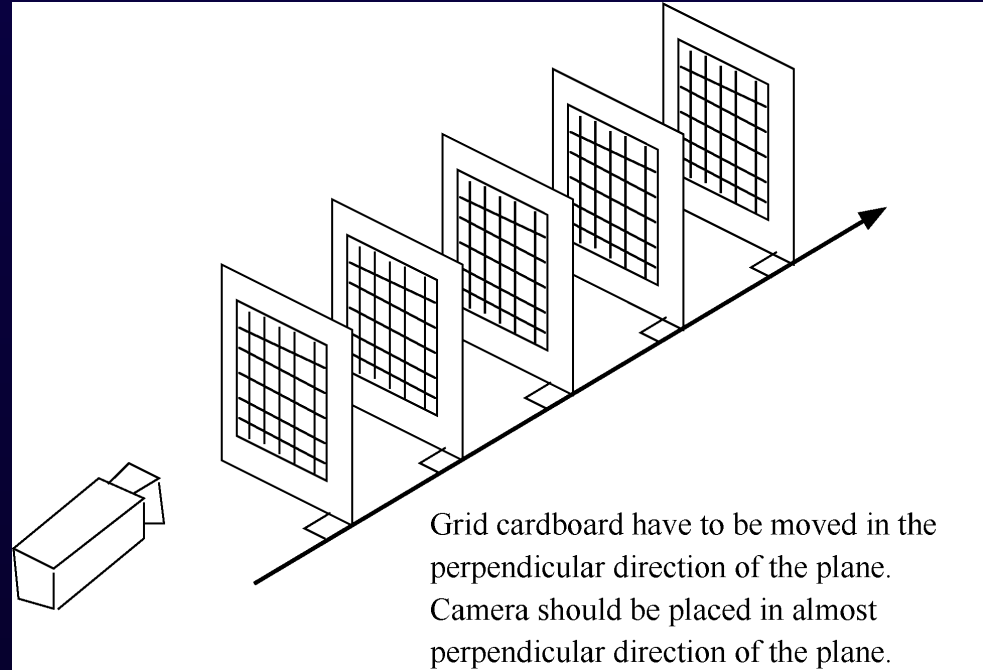
- Take pattern pictures as large as possible.
- Slant in various directions with big angle.
- 4 times or more

## Step2: Getting perspective projection matrix 'calib\_cparam'

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**Manual line-fitting**



## **Easy 1 step method: 'calib\_camera2'**

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- Same operation as 'calib\_dist'.
- Getting all camera parameters including distortion parameters and perspective projection matrix.
- Not require careful setup.
- Accuracy is good enough for image overlay.  
(Not good enough for 3D measurement.)

# Camera Parameter Implementation

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## Camera parameter structure

- ```
typedef struct {  
    int      xsize, ysize;  
    double   mat[ 3][ 4] ;  
    double   dist_factor[ 4] ;  
} ARParam;
```

## Adjust camera parameter for the input image size

- ```
int arParamChangeSize( ARParam *source,  
                      int xsize, int ysize,  
                      ARParam *newparam );
```

## Read camera parameters from the file

- ```
int arParamLoad( char *filename, int num,  
               ARParam *param, ... );
```

## 2.2 Notes on Image Processing

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- **Image size for marker detection**
- **Use of tracking history**
- **Accuracy v.s. Speed on pattern identification**



# (1) Image size for image processing

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## AR\_IMAGE\_PROC\_IN\_FULL

- Full size images are used for marker detection.
- Taking more time but accuracy is better.
- **Not good for interlaced images**

## AR\_IMAGE\_PROC\_IN\_HALF

- Re-sampled half size images are used for marker detection.
- Taking less time but accuracy is worse.
- Good for interlaced images

**External variable: arImageProcMode in 'ar.h'**

**Default value: DEFAULT\_IMAGE\_PROC\_MODE in 'config.h'**

## **(2) Use of tracking history**

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### **Marker Detection**

- **With tracking history: arDetectMarker();**
- **Without tracking history: arDetectMarkerLite();**

### **How to use tracking history**

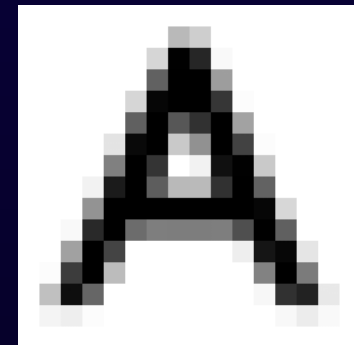
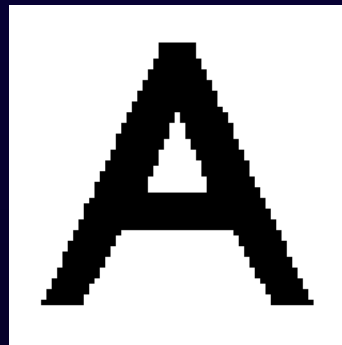
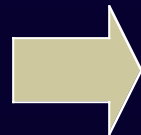
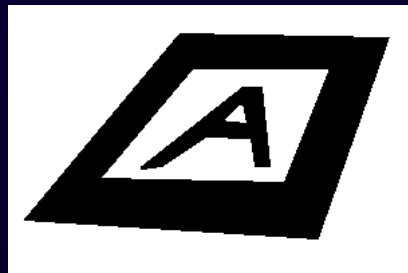
- **Error correction of pattern identification**
- **Lost marker insertion**

# (3) Accuracy v.s. Speed on pattern identification

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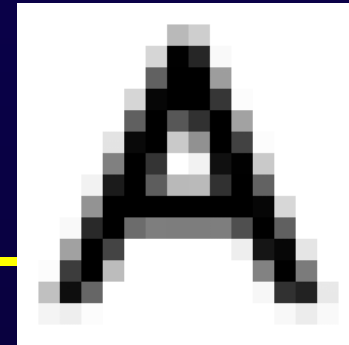
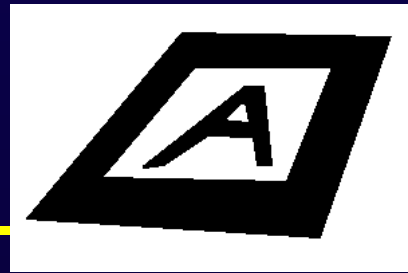
Pattern normalization takes much time.  
This is a problem in use of many markers.

- Normalization process.



Normalization

Resolution convert



In 'config.h'

```
#define AR_PATT_SAMPLE_NUM 64  
#define AR_PATT_SIZE_X 16  
#define AR_PATT_SIZE_Y 16
```

|            | Identification Accuracy | Speed |
|------------|-------------------------|-------|
| Large size | Good                    | Slow  |
| Small size | Bad                     | Fast  |

## 2.3 Pose & Position Estimation

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- **Two types of initial condition**
- **Use of estimation accuracy**

# (1) Two types of initial condition

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## 1. Geometrical calculation based on 4 vertices in screen coordinates

```
double arGetTransMat( ARMarkerInfo *marker_info,  
                    double center[2], double width,  
                    double conv[3][4] );
```

## 2. Use of information from previous image frame

```
double arGetTransMatCont( ARMarkerInfo *marker_info,  
                        double prev_conv[3][4],  
                        double center[2], double width,  
                        double conv[3][4] );
```

- See 'simpleTest2.c'

## (2) Use of estimation accuracy

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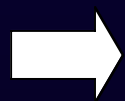
$$\begin{bmatrix} h\hat{x}_i \\ h\hat{y}_i \\ h \end{bmatrix} = \mathbf{C} \cdot \mathbf{T}_{\text{CM}} \begin{bmatrix} X_{Mi} \\ Y_{Mi} \\ Z_{Mi} \\ 1 \end{bmatrix}, \quad i = 1, 2, 3, 4$$

$$err = \frac{1}{4} \sum_{i=1,2,3,4} \left\{ (x_i - \hat{x}_i)^2 + (y_i - \hat{y}_i)^2 \right\}$$

`arGetTransMat()` minimizes the 'err'.

It returns this minimized 'err'.

If 'err' is still big,



Miss-detected marker.

Use of camera parameters by bad calibration.

## 2.4 Background video display

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### Texture mapping v.s. glDrawPixels()

- Performance depends on hardware and OpenGL driver.

**external variable: argDrawMode in 'gsub.h'**

**#define DEFAULT\_DRAW\_MODE in 'config.h'**

- AR\_DRAW\_BY\_GL\_DRAW\_PIXELS
- AR\_DRAW\_BY\_TEXTURE\_MAPPING

**Note: glDrawPixels() dose not compensate image distortion.**

**See 'examples/test/graphicsTest.c' and 'modeTest'**



# Some notes

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- **ARToolKit has limitation as a 3D measurement system because of monocular camera setup.**
- **Lighting conditions and Marker materials are also important.**

# Coming next

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- **In a half year**
  - Stereo version of ARToolKit
- **In a year**
  - Shadow representation with VRML paser
  - Texture tracking (kind of natural feature tracking)